

$$f(x) = \frac{a}{1-r} \quad \text{Find the Sum Formula}$$

Find the interval of Convergence and the function that represents the series

$$24) \sum_{n=0}^{\infty} \frac{(x+1)^{2n}}{9^n} =$$

$$r = \frac{(x+1)^2}{9}$$

$$f(x) = \frac{1}{1 - \frac{(x+1)^2}{9}}$$

$$-1 < \frac{(x+1)^2}{9} < 1$$

$$-9 < (x+1)^2 < 9$$

$$(x+1)^2 < 9$$

$$x+1 < 3 \quad x+1 > -3$$

$$x < 2 \quad x > -4$$

$$\boxed{-4 < x < 2}$$

$$28) \sum_{n=0}^{\infty} \left(\frac{\sin x}{2} \right)^n =$$

$$r = \frac{\sin x}{2}$$

$$f(x) = \frac{1}{1 - \frac{\sin x}{2}}$$

$$-1 < \frac{\sin x}{2} < 1$$

$$-2 < \sin x < 2$$

$$\text{I.O.C } -\infty < x < \infty$$

$$(-\infty, \infty)$$

$$\{x \in \mathbb{R}\}$$

All real #'s

$$(x+1)(x+1)$$

$$f(x) = \frac{9}{9 - (x+1)^2}$$

$$f(x) = \frac{9}{9 - (x^2 + 2x + 1)}$$

$$f(x) = \frac{9}{-x^2 - 2x + 8}$$

What you'll Learn About
 Testing Endpoints for Convergence

Find the Interval
 of Convergence.

$$24) \sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n (x-1)^n =$$

$$\lim_{n \rightarrow \infty} \left| \frac{\left(\frac{2}{3}\right)^{n+1} (x-1)^{n+1}}{\left(\frac{2}{3}\right)^n (x-1)^n} \right| = \left| \frac{2}{3} (x-1) \right| < 1$$

$r = \frac{2}{3}(x-1)$

$$\boxed{-1 < \frac{2}{3}(x-1) < 1} \checkmark$$

$x = 5/2$

$$\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n \left(\frac{5}{2}-1\right)^n$$

$$\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n \left(\frac{3}{2}\right)^n = \sum_{n=0}^{\infty} 1^n = \sum_{n=0}^{\infty} 1$$

$$\lim_{n \rightarrow \infty} 1 = 1 \neq 0$$

$\lim_{n \rightarrow \infty} 1 = 1 \neq 0$

$$-\frac{3}{2} < x-1 < \frac{3}{2}$$

$$\boxed{-\frac{1}{2} < x < \frac{5}{2}}$$

$x = -\frac{1}{2}$

$$\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n \left(-\frac{1}{2}-1\right)^n$$

$$\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n \left(-\frac{3}{2}\right)^n$$

$$\sum_{n=0}^{\infty} (-1)^n \rightarrow \lim_{n \rightarrow \infty} |(-1)^n| \neq 0 \text{ Diverges}$$

$$5) \sum_{n=0}^{\infty} \frac{(-1)^n (3x-1)^n}{n^2} =$$

$$\lim_{n \rightarrow \infty} \left| \frac{(-1)^{n+1} (3x-1)^{n+1}}{(n+1)^2} \cdot \frac{n^2}{(-1)^n (3x-1)^n} \right| = \left| \frac{(3x-1)n^2}{(n+1)^2} \right| = |3x-1| < 1$$

$x=0$

$$\sum_{n=0}^{\infty} \frac{(-1)^n (-1)^n}{n^2}$$

$$\sum_{n=0}^{\infty} \frac{1}{n^2} \quad p=2 > 1$$

$x = \frac{2}{3}$

$$\sum_{n=0}^{\infty} \frac{(-1)^n}{n^2}$$

i) $\lim_{n \rightarrow \infty} \left| \frac{(-1)^n}{n^2} \right| = 0$

ii) $\left| \frac{(-1)^{n+1}}{(n+1)^2} \right| < \left| \frac{(-1)^n}{n^2} \right|$

conditional $-1 < 3x-1 < 1$
 $0 < 3x < 2$

$$\boxed{0 \leq x \leq \frac{2}{3}}$$

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$$\sum_{n=0}^{\infty} \frac{1}{n^2} \quad p=2 > 1 \text{ converges Absolut}$$

I.O.C

$$\lim_{n \rightarrow \infty} \left| \frac{1}{(n+1)^2} \cdot \frac{n^2}{1} \right| = 1$$

Interval of Abs Convergence
 $0 < x \leq \frac{2}{3}$

i) $\lim_{n \rightarrow \infty} \left| \frac{(-1)^n}{\sqrt{n}} \right| = 0$
 ii) $\left| \frac{(-1)^{n+1}}{\sqrt{n+1}} \right| < \left| \frac{(-1)^n}{\sqrt{n}} \right|$

9) $\sum_{n=0}^{\infty} \frac{x^n}{\sqrt{n}} =$

$\lim_{n \rightarrow \infty} \left| \frac{x^{n+1}}{\sqrt{n+1}} \cdot \frac{\sqrt{n}}{x^n} \right| = |x| < 1$

$x = -1$ conditional convergence
 $-1 < x < 1$

$x = -1$
 $\sum_{n=0}^{\infty} \frac{(-1)^n}{\sqrt{n}}$

Absolute? NO

$x = 1$
 $\sum_{n=0}^{\infty} \frac{1}{\sqrt{n}}$ $p = \frac{1}{2} \leq 1$ diverge

13) $\sum_{n=0}^{\infty} \frac{n!}{2^n} x^{2n} =$

$\lim_{n \rightarrow \infty} \left| \frac{(n+1)! x^{2n+2}}{2^{n+1}} \cdot \frac{2^n}{n! x^{2n}} \right| = \lim_{n \rightarrow \infty} \left| \frac{(n+1) x^2}{2} \right| = \infty > 1$

diverges except at the center $x=0$

1) $\sum_{n=0}^{\infty} \frac{(-x)^n}{n!} =$

$\lim_{n \rightarrow \infty} \left| \frac{(-x)^{n+1}}{(n+1)!} \cdot \frac{n!}{(-x)^n} \right| = \lim_{n \rightarrow \infty} \left| \frac{x}{n+1} \right| = 0 < 1$

converges always

$-\infty < x < \infty$