

Using the calculator to compute area

A) $\int_0^{\pi} \frac{1}{5 + 3\cos(x)}$

B) Find the Area of the region between the x-axis and the graph of $y = \sqrt{9 - 4x^2}$.

C) For what value of x does $\int_0^x t^2 dt = 2$

$$\int_0^x t^2 dt = 2$$
$$\left. \frac{1}{3} t^3 \right|_0^x = 2$$

$$(3) \frac{1}{3} x^3 = 2(3)$$

$$x^3 = 6$$
$$x = \sqrt[3]{6}$$

~~$\int e^{-t^3} = e^{-t^3}$~~
 ~~$\frac{d}{dx}(e^{-t^3}) = e^{-t^3} \cdot -3t^2$~~

D) For what value of x does $\int_0^x e^{-t} dt = .5695$

E) Find the area of the region in the first quadrant enclosed by the coordinate axes and the graph of $x^5 + y^5 = 1$.

F) Find the average value of $\sqrt{\sin x}$ on the interval $[1, 2]$.

What you'll Learn About

- Analyzing antiderivatives graphically
- Connecting Antiderivatives to Area
- Taking the derivative of an integral

Long Way
(Proof)

A) Find $\frac{d}{dx} \left[\int_1^x (\cos t) dt \right]$
 $\frac{d}{dx} \left[\sin t \right]_1^x$
 $\frac{d}{dx} [\sin x - \sin 1]$

$$\frac{d}{dx} \int_1^x \cos t dt = \cos x$$

B) Find $\frac{d}{dx} \left[\int_1^{x^3} (\cos t) dt \right]$
 $\frac{d}{dx} \left[\sin t \right]_1^{x^3}$
 $\frac{d}{dx} [\sin(x^3) - \sin 1]$

$$\frac{d}{dx} \int_1^{x^3} \cos t dt = \cos(x^3) \cdot 3x^2$$

C) Find $\frac{d}{dx} \left[\int_{x^3}^{x^2} (\cos t) dt \right]$
 $\frac{d}{dx} \left[\sin t \right]_{x^3}^{x^2}$
 $\frac{d}{dx} [\sin(x^2) - \sin(x^3)]$

$$\frac{d}{dx} \int_{x^3}^{x^2} \cos t dt = \cos(x^2) \cdot 2x - \cos(x^3) \cdot 3x^2$$

Find $\frac{dy}{dx}$ for the given function

$$2) y = \int_2^x (3t + \cos(t^2)) dt$$

$$\frac{dy}{dx} = (3x + \cos(x^2)) \cdot 1 - (3 \cdot 2 + \cos(2^2)) \cdot 0$$

$$\frac{dy}{dx} = (3x + \cos(x^2))$$

$$10) y = \int_6^{x^2} (\cot(3t)) dt$$

$$\frac{dy}{dx} = \cot(3x^2) \cdot 2x$$

$$12) y = \int_{\pi}^{\pi-x} \left(\frac{1 + \sin^2 t}{1 + \cos^2 t} \right) dt$$

$$\frac{dy}{dx} = \left(\frac{1 + \sin^2(\pi-x)}{1 + \cos^2(\pi-x)} \right) \cdot (-1)$$

$$14) y = \int_x^7 (\sqrt{2t^4 + t + 1}) dt$$

$$\frac{dy}{dx} = 0 - \sqrt{2x^4 + x + 1}$$

$$20) y = \int_{\sin x}^{\cos x} (t^2) dt$$

$$\frac{dy}{dx} = (\cos x)^2 \cdot (-\sin x) - (\sin x)^2 \cdot \cos x$$