

What you'll Learn About

- How to find the derivative of a composite function

A) $y = \sin(x)$

$\frac{dy}{dx} = \cos x \cdot 1 = \cos x$
 ↑
 derivative of angle

B) $y = \sin(x^2 - 4)$

$y' = \cos(x^2 - 4) \cdot 2x$
 ↑
 derivative of angle

C) $y = \cos^2(3x)$

$y = [\cos(3x)]^2$

$y' = 2[\cos(3x)]^1 \cdot (-\sin(3x)) \cdot (3)$
 power rule $\frac{d}{dx}$ of trig fct $\frac{d}{dx}$ angle

$y = x^2$
 $y' = 2x^1$

Product rule

→ D) $y = (\csc x)^2 \cot x$

$y' = (\csc x)^2 \cdot (-\csc^2 x) + (\cot x) \left[2 \csc x (-\csc x \cot x) \right]$
 $\frac{d}{dx} (\csc x)^2$

$y' = -\csc^4 x - 2 \cot^2 x \csc^2 x$

$3 \left[2 \cdot 4 - 7 \cdot 5 \right]$

$$E) y = 5\sqrt{\sin(2x) + \cos(2x)}$$

$$y = 5 \left(\sin(2x) + \cos(2x) \right)^{1/2}$$

$$y' = 5 \cdot \frac{1}{2} \left[\sin(2x) + \cos(2x) \right]^{-1/2} \cdot \left(\cos(2x) \cdot 2 - \sin(2x) \cdot 2 \right)$$

power rule

$$E) y = (\sin x + \cos x)^{-2}$$

$$y' = -2(\sin x + \cos x)^{-3} \cdot (\cos x \cdot 1 - \sin x \cdot 1)$$

$$y' = \frac{-2(\cos x - \sin x)}{(\sin x + \cos x)^3}$$

$$F) y = \frac{1}{(\sin(x^3) + \cos(x^3))^4}$$

$$y = (\sin(x^3) + \cos(x^3))^{-4}$$

$$y' = -4 \left[\sin(x^3) + \cos(x^3) \right]^{-5} \cdot \left(\cos(x^3) \cdot 3x^2 - \sin(x^3) \cdot 3x^2 \right)$$

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$$\textcircled{15} \quad y = (\sin x)^{-5}$$
$$\frac{dy}{dx} = -5(\sin x)^{-6} \cdot \cos x \cdot 1$$

$$y = [\cos(7x)]^2$$
$$y' = 2[\cos(7x) \cdot -\sin(7x) \cdot 7]$$