

$$y = \sin^{-1} x$$

Inverse sine

$$y = \arcsin x$$

$$y = \sin(45^\circ)$$

$$\frac{\sqrt{2}}{2} = \sin(45^\circ)$$

↑ ratio ↑ angle

$$y = \sin^{-1}\left(\frac{\sqrt{2}}{2}\right)$$

$$\frac{\pi}{4} = \sin^{-1}\left(\frac{\sqrt{2}}{2}\right)$$

↑ angle ↑ ratio

A) $y = \arcsin(x^2)$ ↑ ratio

$$y = \arcsin(x^2)$$

$$\frac{dy}{dx} = \frac{1}{\sqrt{1-(\text{ratio})^2}} \cdot \frac{d}{dx}(\text{ratio})$$

$$= \frac{1}{\sqrt{1-(x^2)^2}} \cdot 2x = \frac{2x}{\sqrt{1-x^4}}$$

C) $y = x^2 \arccos(\sin x)$

$$y = (x^2)(\arccos(\sin x))$$

$$y' = x^2 \left(\frac{-\cos x}{\sqrt{1-\sin^2 x}} \right) + \arccos(\sin x) \cdot 2x$$

D) $y = x\sqrt{1-x^2} + \arctan\sqrt[3]{x}$

E) $f(x) = \operatorname{arccsc}(5x^3 - \sin x)$

$$y = x(1-x^2)^{1/2} + \arctan(x^{1/3})$$

$$y' = x \left[\frac{1}{2}(1-x^2)^{-1/2} \cdot (-2x) \right] + (1-x^2)^{1/2} + \frac{1}{1+(x^{1/3})^2} \cdot \frac{1}{3} x^{-2/3}$$

Find the equation of the tangent line

F) $y = \csc^{-1} x$ at $x = 2$

$$y = \arccos(x^{-1})$$
 ↑ ratio

B) $y = \arccos\left(\frac{1}{x}\right)$

$$\frac{dy}{dx} = \frac{-1}{\sqrt{1-(x^{-1})^2}} \cdot -|x^{-2}$$

$$\frac{dy}{dx} = \frac{1}{x^2 \sqrt{1-x^{-2}}}$$