

Extreme
value

Determine the maximum and minimum velocity of the function given

2) $v(t) = t^3 - 3t^2 + 4$ $[0, 4]$

$$v'(t) = a(t) = 3t^2 - 6t$$

$$0 = 3t^2 - 6t$$

$$0 = 3t(t - 2)$$

$$t = 0 \quad t = 2$$

$$v(0) = 4$$

$$v(2) = 8 - 12 + 4 = 0$$

$$v(4) = 64 - 48 + 4 = 20$$

$(2, 0)$ Abs Min

$(4, 20)$ Abs Max

Determine the maximum and minimum acceleration of the function given

5) $v(t) = 4t^2 - 6t^3$ $[0, 3]$

$$a(t) = v'(t) = 8t - 18t^2$$

$$a'(t) = 8 - 36t$$

$$0 = 8 - 36t$$

$$\frac{36t}{36} = \frac{8}{36}$$

$$t = \frac{2}{9}$$

$$a(0) = 0$$

$$a\left(\frac{2}{9}\right) = 8\left(\frac{2}{9}\right) - 18\left(\frac{2}{9}\right)^2$$

$$= \frac{16}{9} - \frac{18\left(\frac{4}{81}\right)}{1}$$

$$= \frac{16}{9} - \frac{2\left(\frac{4}{9}\right)}{1}$$

$$= \frac{16}{9} - \frac{8}{9} - \frac{8}{9}$$

$$a(3) = -130$$

Maximize
 Minimize

What you'll Learn About:

How to use derivatives to solve real world problems

$y = \sin x \rightarrow$ height



A) A rectangle is to be inscribed under one arch of the sine curve. What is the largest area the rectangle can have, and what dimensions give that area.

Take derivative of

$A'(.5) = .920 > 0$

$A = lw \quad A = bh$

$A'(1) = -1.066 < 0$

$A = (\pi - 2x) \sin x$

$A'(2.5) = .290 > 0$

$A'(x) = (\pi - 2x)\cos x + \sin x(-2)$

$b = \pi - 2(.710)$

Local Max
 b/c A' changes from $+$ to $-$
 $0 = (\pi - 2x)\cos x - 2\sin x$
 $x = .710, 2.431$ and $A(.710) = 0$

$h = \sin(.710)$

$A = (\pi - 2(.710))(\sin(.710))$

B) A rectangle is to be inscribed between the curve $y = 25 - x^2$ and the x-axis. What is the largest area the rectangle can have, and what dimensions give that area.