

$$(x-1)(x-1)$$

What you'll Learn About
Critical Points/Extreme ValuesFind the
critical points

1) $\frac{dy}{dx} = 0$

Critical points
are possible
local max/min
values

8) $y = \frac{1}{x-1} - \frac{1}{x}$

$$y = (x-1)^{-1} - x^{-1}$$

$$\frac{dy}{dx} = -(x-1)^{-2} + x^{-2}$$

$$0 = \frac{-1(x^2)}{(x-1)^2(x^2)} + \frac{1(x-1)^2}{x^2(x-1)^2}$$

$$0 = -x^2 + x^2 - 2x + 1$$

$$0 = -2x + 1$$

$$\begin{array}{r} +2x \quad +2x \\ \hline \frac{2x}{2} = \frac{1}{2} \end{array} \quad \text{Critical point}$$
$$x = \frac{1}{2}$$

12) $f(x) = 4x - \sqrt{x+1}$

$$f(x) = 4x - (x+1)^{1/2}$$

$$f'(x) = 4 - \frac{1}{2}(x+1)^{-1/2}$$

$$0 = 4 - \frac{1}{2\sqrt{x+1}}$$

$$\begin{array}{r} +\frac{1}{2\sqrt{x+1}} \quad +\frac{1}{2\sqrt{x+1}} \\ \hline \end{array}$$

$$\cancel{2\sqrt{x+1}} \frac{1}{2\sqrt{x+1}} = 4 \cdot 2\sqrt{x+1}$$

$$\frac{1}{8} = \frac{8\sqrt{x+1}}{8}$$

$$\left(\frac{1}{8}\right)^2 = (\sqrt{x+1})^2$$

$$\frac{1}{64} = x+1$$

$$\frac{1}{64} - 1 = x$$

Critical
pt

$$x = \frac{-63}{64}$$

Extreme Values

- Critical Points
- Plug the C.P. and the endpoints of interval into $f(x)$

Determine the extreme values of each function

21) $f(x) = x^2 - 4x + 1$ on $[0, 4]$

$$f'(x) = 2x - 4$$

$$0 = 2x - 4$$

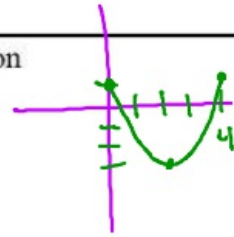
$$2 = x$$

Critical point

$$f(0) = 1$$

$$f(2) = -3$$

$$f(4) = 1$$



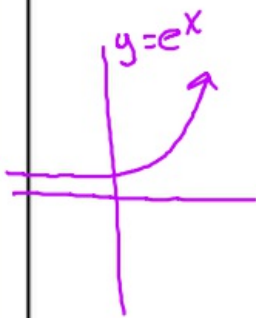
Extreme Values
(0,1) and (4,1) Abs Max
(2,-3) Abs Min

Abs Max

(ln 1.5, 2.25)

Abs Min

(1, $3e - e^2$)



56) $f(x) = 3e^x - e^{2x}$ on $[-.5, 1]$

$$f(x) = 3e^x - e^{2x}$$

$$f'(x) = 3e^x - 2e^{2x}$$

$$0 = 3e^x - 2e^{2x}$$

$$0 = e^x(3 - 2e^x)$$

$$e^x \neq 0 \quad 3 - 2e^x = 0$$

$$\frac{3}{2} = \frac{2e^x}{2}$$

$$\left[-.5, 1\right] \quad \frac{3}{\sqrt{e}} - \frac{1}{e} = \frac{3}{\sqrt{2.7}} - \frac{1}{2.7}$$

$$f(-.5) = 3e^{-.5} - e^{-1} = 1.4$$

$$\begin{aligned} f(\ln 1.5) &= 3e^{\ln 1.5} - e^{2\ln 1.5} \\ &= 3(1.5) - e^{(\ln 1.5)^2} \\ &= 4.5 - (1.5)^2 \\ &= 4.5 - 2.25 \\ &= 2.25 \end{aligned}$$

$$f(1) = 3e - e^2 < 2.25 = 2.25$$

$$\begin{aligned} 1.5 &= e^x \\ \ln(1.5) &= \ln(e^x) \\ \ln(1.5) &= x \quad \text{C.P.} \end{aligned}$$