

Split the middle term

$$ax^2 + bx + c$$

1st multiply a and c together.

2nd find numbers that multiply to get the product from above that add to get b .

3rd replace (or split) the middle term with the 2 numbers from step 2.

4th Group the first 2 terms together and group the second terms together

5th Find the GCF of each set of Parenthesis

6th Write as a product of linear factors

$$4x^2 + 9x + 2$$

$$6x^2 - 11x + 4$$

$$9x^2 + 12x + 4$$

$$12x^2 - 25x + 7$$

$$4x^2 - 4x - 35$$

$$6x^2 + 13x - 25$$

$$\begin{aligned} & 10 \cdot -4 = -40 \\ & 10x^2 + 3x - 4 \quad -8 \cdot 5 \\ & (10x^2 - 5x) + (8x - 4) \quad -5 \cdot 8 \\ & \underline{5x(2x-1)} + \underline{4(2x-1)} \\ & (5x+4)(2x-1) \end{aligned}$$

$$\begin{aligned} & 25 \cdot 4 = 100 \\ & 25x^2 - 20x + 4 \quad -100 \cdot -1 \\ & (25x^2 - 10x) + (10x + 4) \quad -50 \cdot -2 \\ & 5x(5x-2) - 2(5x-2) \quad -25 \cdot -4 \\ & \underline{5x(5x-2)} - \underline{2(5x-2)} \quad -10 \cdot -10 \\ & (5x-2)(5x-2) \quad -20 \cdot -5 \\ & (5x-2)^2 \end{aligned}$$

Both GCF and Split the middle term

$$\begin{array}{r} 4x^2 - 2x - 20 \\ \boxed{2(2x^2 - x - 10)} \\ \underline{-20} \\ \underline{\underline{-5 \cdot 4}} \\ (2x^2 + 4x)(-5x - 10) \\ \underline{-10 \cdot 2} \\ \underline{-2 \cdot 10} \\ 2x(x+2) - 5(x+2) \\ \rightarrow 2(2x-5)(x+2) \end{array}$$

$$\begin{array}{r} -3x^2 + 12x + 15 \\ \underline{-5} \\ \underline{-5 \cdot 1} \end{array}$$

$$-3(x^2 - 4x - 5)$$

$$-3(x-5)(x+1)$$

$$-24$$

$$\begin{array}{r} 2(6x^2 + 5x - 4) \\ \underline{-9} \\ \underline{-6 \cdot 16} \end{array}$$

$$\begin{array}{r} 8x^2 - 28x - 60 \\ \underline{-10 \cdot 3} \end{array}$$

$$\begin{array}{r} 12x^2 + 10x - 8 \\ \underline{-6 \cdot 16} \end{array}$$

$$4(2x^2 - 7x - 15)$$

$$(12x^2 - 6x) + (6x - 8)$$

$$(2x^2 - 10x) + (3x - 15)$$

$$6x(2x-1) + 8(2x-1)$$

$$2x(x-5) + 3(x-5)$$

$$(6x+8)(2x-1)$$

$$4(2x+3)(x-5)$$

$$2(3x+4)(2x-1)$$

$$112x^2 - 168x + 63$$

$$7(16x^2 - 24x + 9)$$

$$(16x^2 - 12x)(-12x + 9)$$

$$4x(4x-3) - 3(4x-3)$$

$$7(4x-3)(4x-3)$$

$$x^2 - 25 \quad 7(4x-3)^2$$

$$x^2 - 49$$

Special Cases

Difference of squares

$$4x^2 - 9$$

$$9x^2 - 1$$