

$$H) \sum_{n=1}^{\infty} \frac{\cos(n\pi)}{2^n} =$$

$$I) \sum_{n=1}^{\infty} \frac{(-1)^n n}{\sqrt{n^2+1}} =$$

$$\frac{1}{3} - \frac{1}{18} + \frac{1}{83} - \frac{1}{256} + \dots$$

$$J) \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^4+2} =$$

Absolute  
Convergence

$$(1) \lim_{n \rightarrow \infty} \left| \frac{(-1)^{n+1}}{n^4+2} \right| = 0$$

$$(2) \left| \frac{(-1)^{(n+1)+1}}{(n+1)^4+2} \right| < \left| \frac{(-1)^{n+1}}{n^4+2} \right|$$

$$K) \sum_{n=1}^{\infty} \frac{(-1)^n}{(1.1)^n}$$

$$\frac{1}{3} + \frac{1}{18} + \frac{1}{83} + \frac{1}{256} + \dots$$

$$\sum_{n=1}^{\infty} \frac{1}{n^4+2} \text{ converges}$$

$$\text{Compare to } \sum_{n=1}^{\infty} \frac{1}{n^4}$$

converges  $p=4 > 1$

$$\lim_{n \rightarrow \infty} \frac{\frac{1}{n^4+2}}{\frac{1}{n^4}} = \frac{n^4}{n^4+2} = 1$$

Conditional  
Convergence

$$8) \sum_{n=1}^{\infty} \frac{(-1)^n e^{1/n}}{n} =$$

$$\textcircled{1} \lim_{n \rightarrow \infty} \left| \frac{(-1)^n e^{1/n}}{n} \right| = 0$$

$$\textcircled{2} \left| \frac{(-1)^{n+1} e^{1/(n+1)}}{n+1} \right| < \left| \frac{(-1)^n e^{1/n}}{n} \right|$$

$$11) \sum_{n=1}^{\infty} \frac{\cos(n\pi)}{n^{3/4}} = \sum_{n=1}^{\infty} \frac{(-1)^n}{n^{3/4}}$$

$$\sum_{n=1}^{\infty} \frac{e^{1/n}}{n} \text{ diverges}$$

compare to  $\sum_{n=1}^{\infty} \frac{1}{n}$

Harmonic

$$\lim_{n \rightarrow \infty} \frac{e^{1/n}}{\frac{1}{n}} = \frac{ne^{1/n}}{1} = 1$$

$$12) \sum_{n=1}^{\infty} \frac{\sin\left(\frac{n\pi}{2}\right)}{n!} = \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n!}$$

$$\lim_{n \rightarrow \infty} \left| \frac{(-1)^{n+1}}{n!} \right| = 0$$

$$\left| \frac{(-1)^{(n+1)+1}}{(n+1)!} \right| < \left| \frac{(-1)^{n+1}}{n!} \right|$$

$$15) \sum_{n=1}^{\infty} \frac{(-1)^n n^n}{n!} =$$

$$\lim_{n \rightarrow \infty} \left| \frac{(-1)^n n^n}{n!} \right| \neq 0$$

$$\sum_{n=1}^{\infty} \frac{1}{n!}$$

Ratio Test

Diverges