

~~This is wrong!!~~

$$y' = (2x)(3x^2 - 1)$$

$$y' = 6x^3 - 2x$$

Using Algebra and the Product Rule to take a derivative

Algebra then Calculus

$$J) y = (x^2 + 3)(x^3 - x)$$

$$y = (x^2 + 3)(x^3 - x)$$

$$y = x^5 - x^3 + 3x^3 - 3x$$

$$y = x^5 + 2x^3 - 3x$$

$$\boxed{\frac{dy}{dx} = 5x^4 + 6x^2 - 3}$$

Calculus then Algebra

$$J) y = (x^2 + 3)(x^3 - x)$$

$$\frac{dy}{dx} = (x^2 + 3)(3x^2 - 1) + (x^3 - x)(2x)$$

$$\frac{dy}{dx} = 3x^4 - x^2 + 9x^2 - 3 + 2x^4 - 2x^2$$

$$\boxed{\frac{dy}{dx} = 5x^4 + 6x^2 - 3}$$

Using Algebra and the Quotient Rule to take a derivative

$$f(x) = \frac{x^3 + 9}{x}$$

$$f(x) = \frac{x^3}{x} + \frac{9}{x}$$

$$f(x) = x^2 + 9x^{-1}$$

$$\boxed{f'(x) = 2x - 9x^{-2}}$$

$$K) f(x) = \frac{x^3 + 9}{x}$$

$$f(x) = \frac{x^3 + 9}{x}$$

$$f(x) = (x^3 + 9) \cdot \frac{1}{x}$$

$$f(x) = (x^3 + 9)(x^{-1})$$

$$f(x) = x^2 + 9x^{-1}$$

$$\boxed{f'(x) = 2x - 9x^{-2}}$$

$$K) f(x) = \frac{x^3 + 9}{x}$$

$$f'(x) = \frac{x(3x^2) - (x^3 + 9)(1)}{(x)^2}$$

$$f'(x) = \frac{3x^3 - x^3 - 9}{x^2}$$

$$f'(x) = \frac{2x^3 - 9}{x^2}$$

$$\boxed{f'(x) = \frac{2x^3}{x^2} - \frac{9}{x^2} \cdot [2x - 9x^{-2}]}$$

Take the Derivative of the function

$$L) y = (x^2 + x + 2)(x^5 + x^3 + 5x)$$

$$y = (x^2 + x + 2)(x^5 + x^3 + 5x)$$

$$\frac{dy}{dx} = (x^2 + x + 2)(5x^4 + 3x^2 + 5) + (x^5 + x^3 + 5)(2x + 1)$$

$$y = x^7 + x^5 + 5x^3 + x^6 + x^4 + 5x^2 + 2x^5 + 2x^3 + 10x$$

$$y = x^7 + x^6 + 3x^5 + x^4 + 7x^3 + 5x^2 + 10x$$

$$\boxed{\frac{dy}{dx} = 7x^6 + 6x^5 + 15x^4 + 4x^3 + 21x^2 + 10x + 10}$$

Take the Derivative of the function

$$M) \quad f(x) = \frac{x^4}{2-x^2}$$

$$f(x) = \frac{x^4}{2-x^2}$$

$$f'(x) = \frac{(2-x^2)(4x^3) - x^4(-2x)}{(2-x^2)^2}$$

$$f'(x) = \frac{8x^3 - 4x^5 + 2x^5}{(2-x^2)^2}$$

$$\boxed{f'(x) = \frac{-2x^5 + 8x^3}{(2-x^2)^2}}$$

$$O) \quad f(x) = \frac{(x+3)(x-4)}{(x+1)(x-3)}$$

$$f(x) = \frac{(x+3)(x-4)}{(x+1)(x-3)}$$

$$f(x) = \frac{x^2 - 1x - 12}{x^2 - 2x - 3}$$

Quotient Rule

$$\frac{1}{3} - 1 = \frac{1}{3} - \frac{3}{3} = -\frac{2}{3}$$

$$N) \quad f(x) = (5-x^2)(3-x)^{-1}$$

$$f(x) = (5-x^2)(3-x)^{-1}$$

$$f(x) = \frac{(5-x^2)}{(3-x)}$$

Quotient Rule

$$P) \quad f(x) = \frac{\sqrt[3]{x} + 1}{\sqrt[3]{x} - 1}$$

$$P) \quad f(x) = \frac{\sqrt[3]{x} + 1}{\sqrt[3]{x} - 1} = \frac{x^{1/3} + 1}{x^{1/3} - 1}$$

$$f'(x) = \left(x^{1/3}\right)\left(\frac{1}{3}x^{-2/3}\right) - \left(x^{1/3} + 1\right)\left(\frac{1}{3}x^{-2/3}\right)$$

$$\text{Algebra} = \frac{1}{3}x^{1/3} - \frac{1}{3}x^{-2/3} - \cancel{\left(\frac{1}{3}x^{1/3} + 1\right)} - \frac{1}{3}x^{-2/3}$$

$$= \frac{-\frac{2}{3}x^{-2/3}}{\left(x^{1/3} - 1\right)^2} - \frac{\left(\frac{-2}{3}x^{2/3}\right)}{\left(\frac{\left(x^{1/3} - 1\right)^2}{1}\right)} = \boxed{\frac{-2}{3x^{2/3}\left(x^{1/3} - 1\right)^2}}$$

$$\boxed{\frac{-2}{3\sqrt[3]{x^2}\left(\sqrt[3]{x}-1\right)^2}}$$