#### CALCULUS: Graphical, Numerical, Algebraic by Finney, Demana, Watts and Kennedy 2.4. Rates of Change pg. 87-94 Chapter 2: Limits and Continuity

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What you'll Learn About

- Average Rates of Change
- A Definition of the Derivative

An object dropped from rest from the top of a tall building fall  $y = 16t^2$  feet in the first t seconds. Find the average speed/average rate of change during the first 2 seconds of flight.

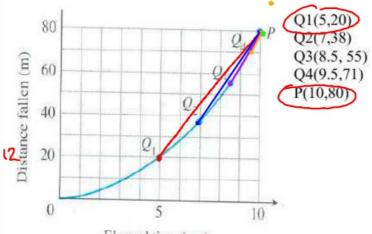
$$t = 0$$
 set  $y = 0$   $f + Avg Speed = 
 $t = 2$  set  $y = 64$   $f + 4$$ 

Find the average rate of change of  $f(x) = \sqrt{4x+1}$  over each interval

$$A.R.O.C = 3-1$$
2-0

Estimate the average rate of change by finding the slopes of each secant line. Indicate units of measure

$$PQ1 = \frac{80 - 20}{60 - 5} = \frac{60}{5}$$

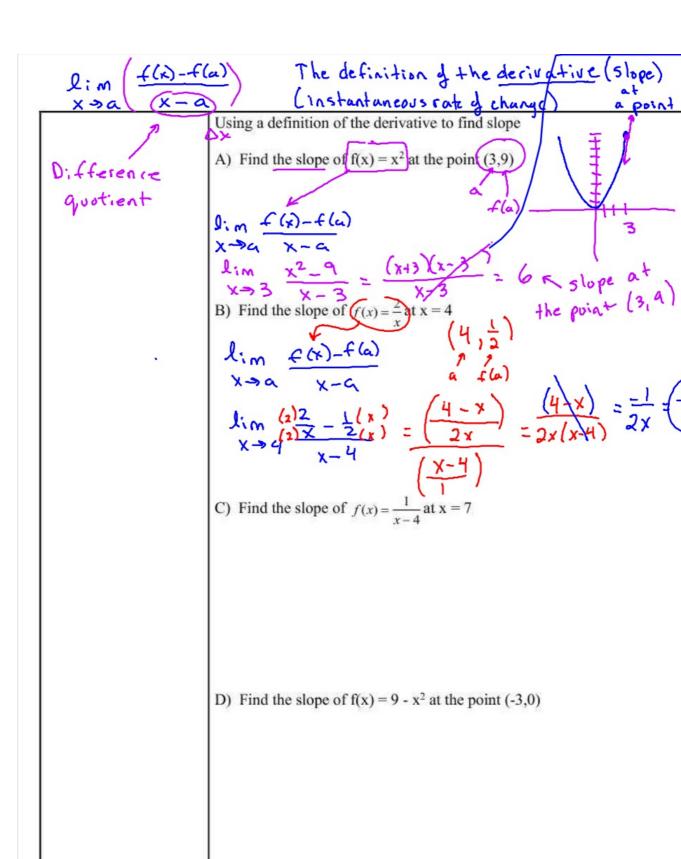


Elapsed time (sec)

Use the slopes of the secant lines to Estimate the instantaneous rate of change/slope at point P

$$\lim_{x \to P} \frac{\Delta y}{\Delta x} = \lim_{x \to Q} \frac{f(x) - f(a)}{x - a}$$

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# CALCULUS: Graphical, Numerical, Algebraic by Finney, Demana, Watts and Kennedy Chapter 3: Derivatives 3.1: Derivative of a function pg. 98-108

What you'll Learn About

- Definition of the derivative
- Notation

Use the substitution h = x - a to create the definition of the derivative

A<sub>1</sub>) Set-up a formula for the slope of  $f(x) = x^2$  at x = -1

A<sub>2</sub>) Use the substitution h = x - a to set-up the definition of the derivative

B<sub>1</sub>) Set-up a formula for the slope of  $f(x) = \frac{1}{x-2}$  at x = 4

 $B_2$ ) Use the substitution h = x - a to set-up the definition of the derivative

Given a definition of the derivative(slope) find the function that you are

taking the derivative of and the point you are finding the derivative(slope) at

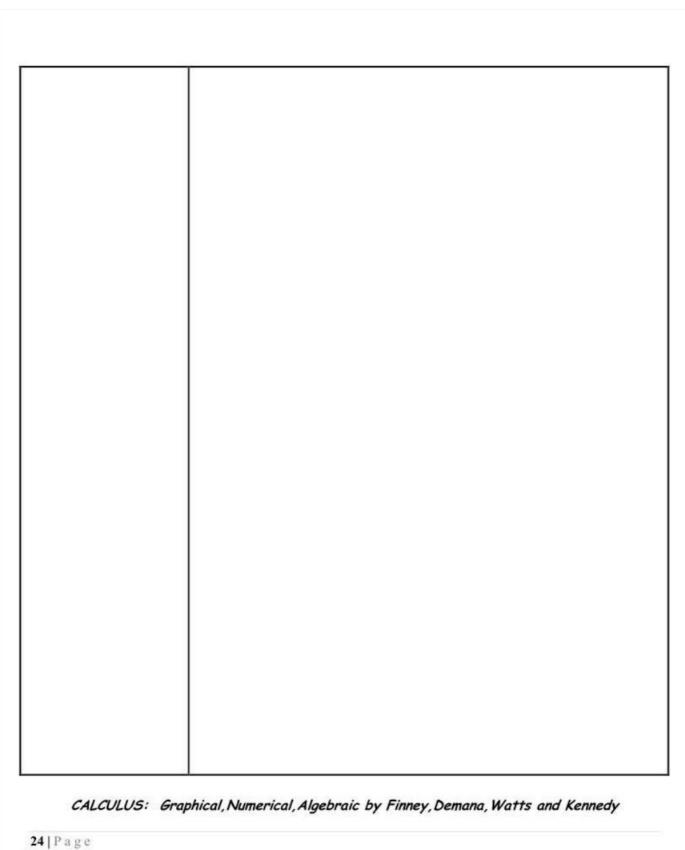
A) 
$$\lim_{x \to 4} \frac{\sqrt{x} - 2}{x - 4}$$

B) 
$$\lim_{x\to 2} \frac{\ln x - \ln 2}{x-2}$$

C) 
$$\lim_{h\to 0} \frac{(2+h)^3-8}{h}$$

D) 
$$\lim_{h \to 0} \frac{\frac{2}{3+h} - \frac{2}{3}}{h}$$

Another Definition:  $\lim_{h\to 0} \frac{f(x+h) - f(x-h)}{2h}$ 

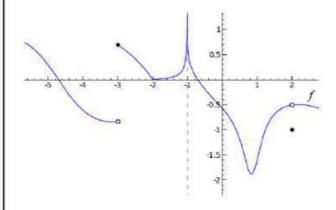


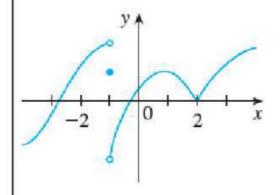
### Chapter 3: Derivatives

# 3.2: Differentiability pg. 109-115

#### What you'll Learn About

- How the derivative might fail to exist
- Differentiability implies local linearity
- Differentiability implies Continuity
  - a. Find all points where the function, f(x), is differentiable.
  - b. Find all points where the function is continuous, but not differentiable.
  - c. Find all points where the graph is neither continuous nor differentiable.





## 3.2 Differentiability:

- b.
- Find all points where the function, f(x), is differentiable. Find all points where the function is continuous, but not differentiable. Find all points where the graph is neither continuous nor differentiable. c.

