

Find the limit of the functions that involve e^x

3. $\lim_{x \rightarrow \infty} \frac{e^{-x}}{x}$

$$\lim_{x \rightarrow -\infty} \frac{e^{-x}}{x}$$

A) $\lim_{x \rightarrow \infty} \frac{e^x + 2x}{2x} =$

B) $\lim_{x \rightarrow -\infty} \frac{e^x + 2x}{2x} =$

Find the limit of the functions that involve sine and cosine

C) $\lim_{x \rightarrow -\infty} \frac{x^3 + \cos x}{x^3}$

D) $\lim_{x \rightarrow +\infty} \frac{x^3 + \cos x}{x^3}$

E) $\lim_{x \rightarrow \infty} \sin\left(\frac{1}{x}\right)$

F) $\lim_{x \rightarrow \infty} \frac{\sin\left(\frac{1}{x}\right)}{1 + \frac{1}{x}}$

Find the limit of the functions that involve absolute value

8A) $\lim_{x \rightarrow \infty} \frac{5x - 2}{|x| - 1}$

8B) $\lim_{x \rightarrow -\infty} \frac{5x - 2}{|x| - 1}$

53A) Find the limit of $f(x)$ as

- a) $x \rightarrow -\infty$, b) $x \rightarrow \infty$, c) $x \rightarrow 0^+$, d) $x \rightarrow 0^-$, e) $x \rightarrow 1^-$, f) $x \rightarrow 1^+$

$$\lim_{x \rightarrow -\infty} \frac{3x-1}{2x+5} = \frac{3}{2}$$

$$\lim_{x \rightarrow \infty} \frac{2}{x-1} = 0$$

$$\lim_{x \rightarrow 0^+} \frac{2}{x-1} = \infty$$

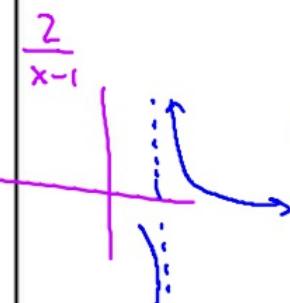
$$\lim_{x \rightarrow 0^-} \frac{2}{x-1} = -\infty$$

$$\lim_{x \rightarrow 1^-} \frac{2}{x-1} = -2$$

$$\lim_{x \rightarrow 1^+} \frac{2}{x-1} = \infty$$

If $f(x) = \begin{cases} \frac{3x-1}{2x+5} & x < 0 \\ \frac{2}{x-1} & x \geq 0 \end{cases}$

left Right



55A) Sketch a graph of a function that satisfies the following conditions.

$(0, 2)$ $\leftarrow \lim_{x \rightarrow 0^+} f(x) = 2$

V.A. $x = -2$

$\leftarrow \lim_{x \rightarrow -2^-} f(x) = \infty$

$\leftarrow \lim_{x \rightarrow -2^+} f(x) = -\infty$

H.A. $y = 2$

$\leftarrow \lim_{x \rightarrow -\infty} f(x) = 2$

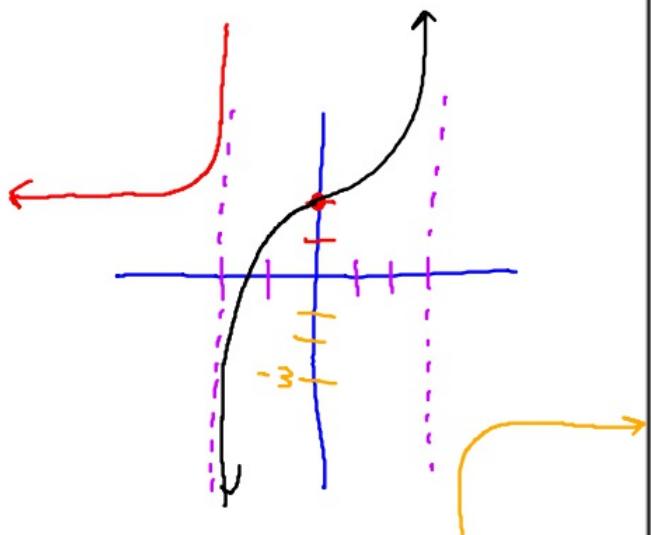
H.A. $y = -3$

$\leftarrow \lim_{x \rightarrow \infty} f(x) = -3$

V.A. $x = 3$

$\leftarrow \lim_{x \rightarrow 3^-} f(x) = \infty$

$\leftarrow \lim_{x \rightarrow 3^+} f(x) = -\infty$



Find the limit of the functions using the sandwich theorem

Example 9 (p.65)

$$\lim_{x \rightarrow 0} \left[x^2 \sin\left(\frac{1}{x}\right) \right] = 0$$

$$0^2 \sin\left(\frac{1}{0}\right)$$

p.76 $0 \times (\text{Between -1 and 1})$

$$10) \lim_{x \rightarrow \infty} \frac{1 - \cos x}{x^2} = 0$$

$$12) \lim_{x \rightarrow \infty} \frac{\sin(x^2)}{x} = \frac{\text{Between -1 and 1}}{x} = 0$$

P.76 53-56, 61, 64

P.76 1, 9, 11, 23

P.68 59-62