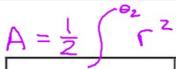


2005 BC2 (Calculator)

The curve above is drawn in xy-plane and is described by the equation in polar coordinates $r = \theta + \sin(2\theta)$ for $0 \le \theta \le \pi$, where r is measured in meters and θ is measured in radians. The derivative of r with respect to θ is given by $\frac{dr}{d\theta} = 1 + 2\cos(2\theta)$.

- a. Find the slope of the curve at the point $\theta = \frac{\pi}{2}$.
- c. Find the angle θ that corresponds to the point on the curve with x-coordinate -2.
- d. For $\frac{\pi}{2} < \theta \le \frac{2\pi}{3}$, $\frac{dr}{d\theta}$ is negative. What does this fact say about r? What does this fact say about the curve?

e. Find the value of θ in the interval $0 \le \theta \le \frac{\pi}{2}$ that corresponds to the point on the curve in the first quadrant with greatest distance from the origin. Justify your answer.



Find the area inside one loop of $r = \sin 3\theta$.

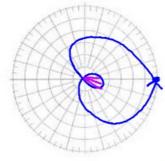
 $A = \frac{1}{2} \int (\sin 3\theta)^2$

 $A = \frac{1}{2}(2) \left(\pi lb \left(\sin 3\theta \right)^2 \right)$

$$3e = 0, \pi, 2\pi$$

$$3\theta = \frac{2}{\pi} \sqrt{3\pi}$$

$$\phi = \frac{11}{6}, \frac{11}{2}$$



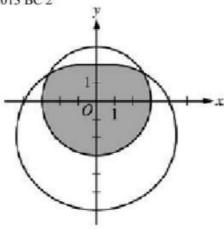
Find the area inside the inner loop of
$$r = 2\cos(\theta) + 1$$
.

$$A = \frac{1}{2} \int_{\frac{2\pi}{3}}^{4\pi/3} \left(2\cos\theta + 1 \right)^2$$

Find the area inside one loop of $r^2 = 2\sin(2\theta)$.

$$A = \frac{1}{2} \int_{0}^{\pi/2} 2 \sin(2x)$$

2013 BC 2



The graphs of the polar curves r = 3 and $r = 4 - 2\sin\theta$ are shown in the figure above. The curves intersect when $\theta = \frac{\pi}{6}$ and $\theta = \frac{5\pi}{6}$.

- Let S be the shaded region that is inside the graph of r = 3 and also inside the graph of $r = 4 - 2\sin\theta$. Find the area of S.
- A particle moves along the polar curve $r = 4 2\sin\theta$ so that at time t seconds, $\theta = t^2$ Find the time t in the interval $1 \le t \le 2$ for which the x-coordinate of the particle's position is -1.

$$\chi = \Gamma(050)$$

 $\chi = (4-2\sin\theta)\cos\theta$
 $-1 = (4-2\sin(t^2)\cos(t^2))$

For the particle described in part (b), find the position vector in terms of t. Find the velocity vector at time t = 1.5.

53.	A region R in the xy-plane is bounded below by the x-axis and above by the
	1
	polar curve defined by $r = \frac{4}{r}$.
	polar curve defined by $r = \frac{4}{1+\sin\theta}$.

Find the area of R by evaluating an integral in polar coordinates.

b. Find the slope of the polar curve when $\theta = \frac{\pi}{2}$